

# Homework #3 (2024 Spring, EE 171)

- ◆ Deadline: June 10<sup>th</sup> 8:00 a.m.
- ◆ Please submit your homework through Gradescope (Course Entry Code: 3PV4VP)
- ◆ Handwriting is not suggested, and a poor format will lose at most 10% of your final score.
- ◆ Giving your solution in English, solution in Chinese is not allowed.
- ◆ Plagiarism is not allowed. Those plagiarized solutions will get 0 point.
- ◆ **Total: 180 points**

Q1. Passive rectifier circuit. In the passive rectifier circuit of Fig. 1,  $L$  is very large, such that the inductor current  $i(t)$  is essentially dc. All components are ideal. **(80 points)**

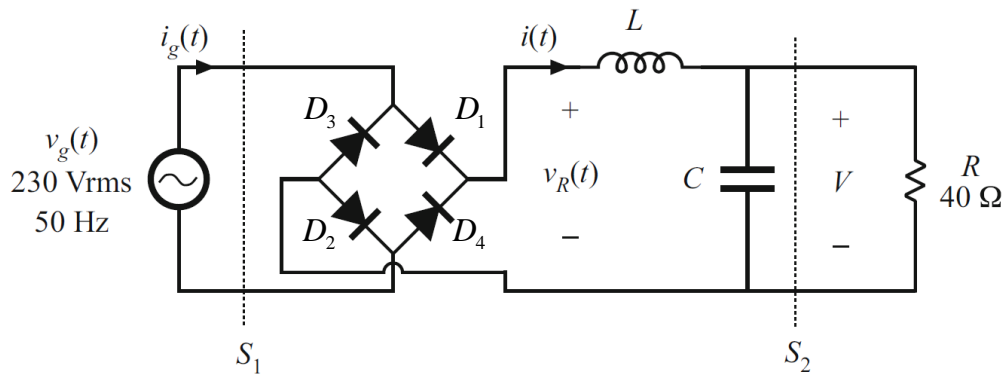


Fig. 1 Passive rectifier circuit

- (a) Determine the power factor, measured at surfaces  $S_1$  and  $S_2$ . **(20 points)**
- (b) Replace  $D_1$  and  $D_3$  with thyristor  $Q_1$  and  $Q_3$ , the thyristor delay angle is  $\alpha$ . Analyze the operation mode. Sketch the waveforms  $v_R(t)$  and  $i_g(t)$ ; Label the conduction intervals of each thyristor and diode. **(40 points)**
- (c) Derive an expression for the output voltage  $V$ , as a function of the rms line-line voltage and the delay angle. Derive an expression for the power factor. **(20 points)**

Q2. The voltage  $v$  across a load and the current  $i$  into the positive-polarity terminal are as follows (where  $\omega_1$  and  $\omega_3$  are not equal):

$$v(t) = V_d + \sqrt{2}V_1 \cos(\omega_1 t) + \sqrt{2}V_1 \sin(\omega_1 t) + \sqrt{2}V_3 \cos(\omega_3 t) \quad \text{V}$$

$$i(t) = I_d + \sqrt{2}I_1 \cos(\omega_1 t) + \sqrt{2}I_3 \cos(\omega_3 t - \phi_3) \quad \text{A}$$

Calculate the following:

- (a) The average power  $P$  supplied to the load. **(10 points)**
- (b) The rms value of  $v(t)$  and  $i(t)$ . **(20 points)**
- (c) The power factor at which the load is operating. **(10 points)**

Q3. In the circuit Fig. 2,  $v_{s1}$  and  $v_{s2}$  have an rms value of 120V at 60Hz, and the two are  $180^\circ$  out of phase. Assume  $L_s=5\text{mH}$  and  $I_d=10\text{A}$  is a dc current. For the following two values of the delay angle  $\alpha$ , (i)  $45^\circ$  and (ii)  $135^\circ$ .

(a) Obtain  $v_{s1}$ ,  $i_{s1}$  and  $v_d$  waveforms. **(30 points)**

(b) Calculate the average value  $V_d$  and the commutation interval  $u$  **(30 points)**

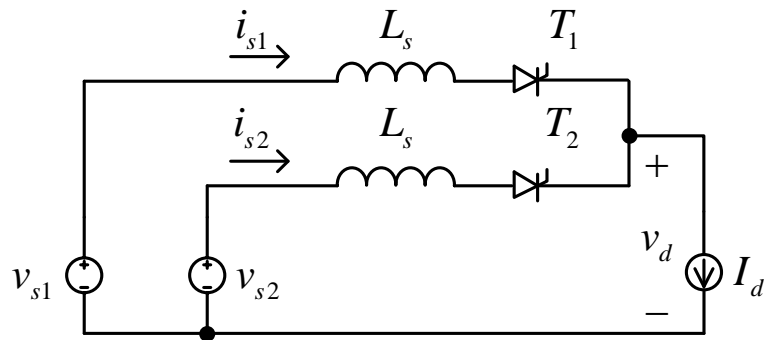


Fig. 2